A Multi-message and Multi-receiver Hybrid Signcryption Scheme for CATV Network

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Abstract

Recently, many multi-receiver signcryption schemes have been proposed. However, few schemes can send multi- messages to multi-receivers, which is an important requirement for the cable television (CATV) networks. In this paper, to cope with the above problem, we present a multi-message and multi-receiver hybrid signcryption scheme based on the assumptions of a discrete logarithm and Gap Diffie Hellman. Our scheme makes it impossible that an attack derives the plaintext or forges signatures. The accuracy and efficiency of the new scheme are analyzed. There is no pairings computation in the proposed scheme. We prove that our scheme is secure against adaptive chosen ciphertext attack and existentially unforgeable against a chosen message attack. Finally, we present a broadcast service protocol for CATV network by employing our proposed scheme.

Keywords: Hybrid Signcryption, Discrete Logarithm, Provable Security, Multi-receiver, Multi-message, CATV network

1. Introduction

Nowadays, as the computational power of the system and the communicational technology are growing rapidly, the demand of highly secured cryptographic system shows its requirement. In general, the communication channel is considered to be insecure in a typical communication system. Confidentiality, integrity and authentication are the most desirable features in a cryptographic system. To achieve these goals, in traditional approaches, the information is digitally signed and then encrypted before transmitting over an unsecure channel. This two-step approach is called-signature encryption. However, this approach is inefficient. In 1997, Y. Zheng combined these two steps into one and proposed a new scheme called signcryption [1]. Zheng's scheme is to perform signature and encryption in a logical step with the cost significantly lower than the traditional signature-then-encryption approach. Since then, many signcryption schemes have been proposed [2-4]. However most signcryption schemes limit the message space to a particular group, which should be restricted while ones want to encrypt arbitrary messages, and almost these schemes are based on public-key encryption technology.

In 2003, Cramer and Shoup gave the formal definition of the KEM-DEM, and, meanwhile, they made an famous construction of KEM-DEM [5]. Then Abe *et al* conducted in-depth research on KEM-DEM hybrid encryption structure [6,7]. The KEM-DEM consists of two parts: One is called key encapsulation technology (KEM) which uses the public key encryption algorithm to generate the ciphertext of the symmetric key; another is called data encapsulation technology (DEM) which uses an encryption key of KEM to encrypt the message with a symmetric encryption algorithm. In the KEM-DEM hybrid encryption structure, there is no limit to the size of plaintext, and the actual data packet of arbitrary length can be encrypted. In 2004, by combining the concepts of hybrid cryptosystem and signcryption and expanding the KEM-DEM structure, Dent [8] proposed the concept of hybrid signcryption and gave its formal definition and secure proof. The hybrid signcryption consists of two parts: One is a signcryption key encapsulation mechanism which uses public key techniques to encapsulate a symmetric key K; the other is a data encapsulation mechanism which employs a symmetric encryption scheme to encrypt a message using the key K. Since then, many schemes have been proposed [9-11]. However, almost in these hybrid signcryption schemes, only two participators are involved and only one message to be encrypted.

Cable television (CATV) network is an efficient, affordable and integrated network. It provides a great variety of services for millions of households, including public channels, specialty channels, data broadcasting, video on demand (VOD), video conferencing, TV commercials, and so on. Recently, in addition to the traditional services, a lot of value-added services based on the CATV network have being developed rapidly. These new services, including information services, e-government, e-commerce, e-dean and smart home, are financial and educational to enhance greatly the ability of the cable network [12].

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With the increasing of the application of cable TV industry, CATV network is facing a great challenge to protect privacy and right of users. When a user buys a type of services provided by the CATV network, the user is an authorized user. It is hoped that only authorized users can enjoy its services in the CATV network. Meanwhile, it is unfair for authorized user if an unauthorized user easily gets related services. Therefore, these broadcasts information must be encrypted to ensure that only authorized users can decrypt the information correctly. In addition, in order to avoid getting some bored services or advertising messages, authorized users should verify the received broadcast messages. If an emergency situation exists, authorized users want to be able to enjoy priority to get the right services. In 2005, based on multi receiver, Smart [13] proposed an efficient key encapsulation scheme to meet the requirements of CATV user. The Smart's scheme is a hybrid cryptosystem, so it can not only ensure the indistinguishability of ciphertext, but also realize efficiently key encapsulation to multiple recipients. Sun *et al* proposed an identity-based multi-receiver signcryption KEM in 2011[14]. This scheme is more effective and practical than other traditional ones, especially when it can be used for network security services such as the securities of broadcast and multicast. However, since CATV can supply some different services, it becomes an urgent requirement that many different messages send to multiple users in one communication. Unfortunately, it cannot be implement by [13,14], their schemes only encrypt single message. Liren Feng *et al* [15] proposed a multi-hybrid signcryption in 2013, this scheme improved KEM-DEM construction, but it can only send the same message to multiple recipients. In the same year, Jing Qiu *et al* [16] proposed a multi-message and multi-receiver ID-based signcryption scheme for rekeying in ad hoc networks. Therefore, the scheme can achieve simultaneously signcrypt *n* message to *n* receivers, but there are a lot of bilinear pairings operation, increasing the computational overhead of communication. Besides, Qiu's scheme still belongs to the public key encryption system. Its computing speed is much lower than the hybrid signcryption system when a long message is signcrypted.

In view of the above facts, we present a new multi-message and multi-receiver hybrid signcryption scheme for CATV networks. It can implement broadcast multiple messages to multiple recipients. Under the random oracle model, we show that the scheme is not only indistinguishable of ciphertext against adaptive chosen ciphertext attacks, but also existentially unforgeable against chosen message attacks. Finally, an analysis of this scheme indicates that it has a lower computation and communication overhead and ensures the security, reliability, public verifiability and the integrality of messages. In the new scheme, all receivers have the same ciphertext set. Therefore, when the ciphertext message is lost or an error is occurred during transmission, all of the receivers cannot properly decrypt the ciphertext message, or ciphertext can be decrypted correctly. Thus, the scheme can ensure the fairness of the decryption.

The rest of this paper is organized as follows:Section 2 and Section 3 introduces the preliminaries which will be used in our scheme and security definitions. The multi-messages and multi-receiver scheme will be present in Section 4 and Section 5. The secure proofs are shown in the Section 6. In Section 7, we present a protocol for CATV networks using the proposed scheme. Finally, we give a concluding to remark this paper in S?ection 8.

2. Preliminaries

2.1 Secure Notions

The securities of our scheme are based on the following secure assumptions and NP-problems.

Let G_1 be a cyclic group generated by g, whose order is a prime $q, G_1 \in Z_p^*$, p is a large prime number.

Definition 1. (Discrete Logarithm (DL) Problem). The DL problem is, $q \mid p-1$, for $d \in G_1$; to looking for a ($0 \le a \le q$, a is satisfied $g^a = d$).

We say that a polynomial-time adversary A breaks DL problem in G_1 if A runs in time at most t and $Adv_A^{DL} \ge \varepsilon$. where $Adv_A^{DL} = pr\lfloor A(g,d,g^a = d) = a, d \in G_1, 0 \le a \le q \rfloor$.

Definition 2. (Gap Diffie-Hellman (GDH) Problem). The GDH problem is, given $g, g^a, g^b \in G_1$, for unknown $a,b \in Z_p^*$, to compute g^{ab}.

We say that a polynomial-time adversary A breaks GDH problem in G_1 if A runs in time at most t and $Adv_A^{GDH} \ge \varepsilon$, where

$$Adv_A^{GDH} = pr\lfloor A(g,g^a,g^b) = g^{ab}, a,b \in Z_p^* \rfloor.$$

2.2 A Review of a Multi Receiver Hybrid Signcryption Scheme

In this section, we will briefly review a multi-receiver Hybrid Signcryption scheme. The detail is in reference [1].

Setup: System randomly chooses a security parameter $k \in N$, a large prime number p and a prime number q ($q \mid p-1$). Let $h_1 : \{0,1\}^* \to \kappa$, $h_2 : \{0,1\}^* \to Z_q^*$ be two cryptographic hash functions, where κ is the length of the key. Let g is an element of order q in Z_p^*. The system parameters are $params = (p,q,g,h_1,h_2)$.

SKeyGen: Given params, KGC generates a public / private key pair of sender (pk_s, sk_s), where $sk_s \in Z_P^*$, $pk_s = g^{sk_s} \bmod p \in Z_P^*$, the (pk_s, sk_s) is sent to the sender and pk_s is publicly.

RKeyGen: Given params, KGC generates *n* public / private key pairs of receivers $(pk_{r1}, sk_{r1}).....,(pk_{rn}, sk_{rn})$, where $sk_{ri} \in Z_P^*$, $pk_{ri} = g^{sk_{ri}} \in Z_P^*$, （i=1,2,……,n）, KGC sends these *n* public / private key pairs to the appropriate receivers and publish all public key $pk_{r_1}, \cdots, pk_{r_n}$.

Signcrypt: Assume a sender wants to signcrypt a messages *m* to *n* different receivers, the sender does the following steps:

1). Pick an integer $x \in Z_p^*$ and compute $z \equiv g^x \bmod p$.

2). Compute $r = h_1(m, z)$ and $K = h_2(r)$.

3). Compute $C = Enc_K(m)$.

4). Compute $s \equiv x/(r + sk_s) \bmod q$.

5). Output ciphertext $\sigma = (C, r, s)$.

Unsigncrypt: On receiving ciphertext $\sigma = (C, r, s)$, every receiver performs the following steps:

1). Compute $z \equiv (pk_s \cdot g^r)^s \bmod p$.

2). Compute $K = h_2(r)$, $m = Dec_K(C)$.

3). Compute $r' = h_1(m, z) \bmod p$, test whether $r' = r$ or not; if it is true, message *m* is correct; otherwise, the communication is stopped.

3. Security Defintions

Definition 3(Confidentiality) · A multi-receivers signcryption scheme is semantically secure against adaptive chosen ciphertext attack (IND-M-HSC-CCA2) if no polynomial bounded adversary has a non-negligible advantage in the following game：

1).The challenger runs keygen to generate multiple key pairs (pk_s, sk_s), $(pk_{r1}, sk_{r1}),(pk_{r2}, sk_{r2}),.....,(pk_{rn}, sk_{rn})$, and all private keys are kept secretly while all public keys are given to adversary A.

2). In the first stage，A makes a number of queries to the following oracles：

- Signcryption oracle：A provides a message $m \in M$ and quires the result of the operation $Signcrypt(params, m, pk_s, sk_s, pk_{r1}, pk_{r2},....., pk_{rn})$

- Unsigncryption oracle：A provides a ciphertext σ and an arbitrary public key pk_u, and quires the result of the operation $Unsigncrypt(params, \sigma, pk_u, pk_{ri}, sk_{ri})$

These queries can be asked adaptively：each query may depend on the answers to previous ones.

3). A provides two plaintexts m_0，$m_1 \in M$. The challenger picks a bit $b \in_R \{0,1\}$ and computes a signcryption $\sigma^* = Signcrypt(m_b, params, pk_s, sk_s, pk_{r1}^*,....., pk_{rn}^*)$. σ^* is sent to A as a challenge ciphertext.

4). A makes a number of new queries as in the first stage with the restriction that it can't query the unsigncryption oracle with σ^*.

5). At the end of the game, A outputs a bit b' and wins if b'=b. A's advantage is defined to be $Adv_A = |\Pr(b' = b) - 1/2|$.

Definition 4 (Unforgeabitity) A multi-receivers signcryption scheme is existentially unforgeable against a chosen message attack (EUF-M-HSC-CMA) if no polynomial bounded adversary F has a non-negligible advantage in the following game：

1). The challenger runs keygen to generate multiple key pairs (pk_s, sk_s), $(pk_{r1}, sk_{r1}),(pk_{r2}, sk_{r2}),.....,(pk_{rn}, sk_{rn})$, all private keys are kept secret while all public keys are given to forger F

2). The forger F makes a number of queries to the signcryption oracle as the confidentiality game. These queries can also be produced adaptively. Note that we allow F to access to all recipients' private keys as well as the corresponding public keys.

3). At the end of the game，F produces a ciphertext σ^* and wins the game if the result of $Unsigncrypt(\sigma^*, pk_u, sk_{ri})$ $(1 \le i \le n)$ is not the " $\perp$ " symbol and signcryption query $Signcrypt(m, sk_u, pk_{r1}, pk_{r2},....., pk_{rn})$ is not made during the game.

Note that there is no need to require the unsigncryption query since the adversary can simulate the unsigncryption oracle by himself.

4. Formal Definition of New Scheme

4.1 Key Encapsulation Mechanism of Multi-message and Multi-receiver (M-KEM)

We present a new key encapsulation mechanism for multiple messages and multiple receivers (M-KEM). Compared with the multi-key encapsulation mechanism (SKM) in the reference [15], the difference is that *the* new scheme is a key

encapsulation based on multi-message. A M-KEM scheme consists of the following five algorithms:

1). Setup: k is a security parameter, the algorithm inputs 1^k, and outputs system parameters *params*.

2). The sender key generation algorithm (*SKeyGen*): the algorithm inputs *params*, and outputs the sender's public / private key pair (pk_s, sk_s).

3). The receivers key generation algorithm (*RKeyGen*): the algorithm inputs *params*, and outputs the receivers' public / private key pairs $(pk_{r1}, sk_{r1}), (pk_{r2}, sk_{r2}), ..., (pk_{rn}, sk_{rn})$.

4). Key encapsulation algorithm (*Encap*): this algorithm inputs system parameters *params*, the private key sk_s, message *m* and (pk_{r1}, pk_{r2},....., pk_{rn}) , and outputs symmetric key *K* and key encapsulation ω, where m is obtained by blending with many different messages.

5). Key decapsulation algorithm (Decap): This algorithm inputs system parameters params, a sender's public key pk_s, receiver's private key sk_{ri} $(1 \le i \le n)$ and a key encapsulation ω, and outputs a symmetric key K or an error symbol " $\perp$ ".

4.2 Data Encapsulation Mechanism (DEM)

The formal analysis of the KEM-DEM originates from Gramer and Shoup's work [5], the key to the KEM-DEM lies in separating the cryptosystem from the different components, which allows modular design cryptosystem. Since then, many expanded or improved KEM mechanism have been proposed [6-8], and the DEM is still a symmetric encryption technique and keeps the original DEM definition. Therefore, this paper also uses the definition of DEM in reference [5], and it is described as follows:

1). Symmetric encryption algorithm (Enc): this algorithm inputs a symmetric key K and the message m, where m is obtained by blending with many different messages $m_1, ..., m_n$, and outputs a ciphertext $C = Enc_K(m)$.

2). Symmetric decryption algorithm (Dec): this algorithm inputs a symmetric key K and the ciphtext C, and outputs a message $m = Dec_K(C)$.

4.3 Definitions of Multi-message and Multi-Receiver Hybrid Signcryption (M-HSC)

The main purpose of the new scheme is confidentially and authentically to broadcast several different messages to multiple receivers, and ensures each receiver is fair, alone unsigncrypt message to get their own plaintext. The M-HSC scheme consists of M-KEM, DEM, setup, *SKeyGen*, *RKeyGen*, signcrypt and unsigncrypt. The detail is described as follows:

Setup: same as the *setup* algorithm in the M-KEM scheme;

SKeyGen: same as the *SKeyGen* algorithm in the M-KEM scheme;

RKeyGen: same as the *RKeyGen* algorithm in the M-KEM scheme;

Signcrypt: inputs $(params, pk_s, sk_s, pk_{r1}, pk_{r2}, \cdots\cdots, pk_{rn})$ and messages $m_1, \cdots, m_n$, where m_i will be send to the *i* receiver for $1 \le i \le n$. The sender calculates ciphertext σ by performing the following steps.

1). Blend *n* message $m_1, \cdots, m_2$ to get message m, where m_i is corresponding to the receiver i.

2). Compute (K, ω) by using the *Encap* algorithm of M-KEM;

3). Compute ciphertext *C* by using the *Enc* algorithm of DEM;

4). Output $\sigma \leftarrow (C, \omega)$.

Unsigncrypt: Inputs $(params, \sigma, pk_s, pk_{ri}, sk_{ri})(1 \le i \le n)$, and each receiver performs the following steps.

1). Compute *K* by using the *Decap* algorithm of M-KEM;

2). Compute *m* by using the *Dec* algorithm of DEM;

3). Check whether the relevant verification equation is hold or not. If it is true, the receiver accepts *m*, otherwise outputs symbol " $\perp$ ";

4). Using its private key, the receiver calculates x_i, and then obtains message m_i.

5. A New Multi-message and Multi-receiver Hybrid Signcryption Scheme

5.1 The proposed scheme

In this section, we present an efficient and secure multi-message and multi-receiver hybrid signcryption scheme based on the discrete logarithm. The following shows the details of the scheme.

Setup: Input a security parameter $k \in N$, and KGC chooses the system parameters which include cyclic group G_1 of prime order $q \ge 2^k$, a generator $g \in G_1$ and a large prime number *p*. The KGC also chooses cryptographic hash functions $h_1 : \{0,1\}^l \to G_1$, $h_2 : \{0,1\}^{l^*} \to G_1$, $h_3 : \{0,1\}^l \to G_1$, where *l* is the length of the computed hash, and l^* is the length of the key. The system parameters are $params = (G_1, g, q, p, h_1, h_2, h_3)$.

SKeyGen: Given *params*, KGC generates a public/ private key pair of sender (pk_s, sk_s), where $sk_s \in Z_P^*$, $pk_s = g^{sk_s} \bmod p \in Z_P^*$, and the (pk_s, sk_s) is sent to the sender and pk_s is public.

RKeyGen: Given *params*, KGC generates *n* public / private key pairs of receivers (pk_{r1}, sk_{r1}), $(pk_{r2}, sk_{r2}), \ldots\ldots, (pk_{rn}, sk_{rn})$, where $sk_{ri} \in Z_P^*$, $pk_{ri} = g^{sk_{ri}} \in Z_P^*$, （$i=1,2,\ldots\ldots,n$）, and KGC send these *n* public / private key pairs to the appropriate receivers and publish all public key $pk_{r1}, pk_{r2}, \ldots\ldots, pk_{rn}$.

Signcrypt: Suppose a sender wants to signcrypt messages $m_1, m_2, \ldots\ldots, m_n$ to *n* different receivers, and the sender does the followings:

1). Choose *r*, $x \in Z_P^*$ and compute $\delta = g^r \bmod p$.

2). Compute $x_i = h_1(pk_{ri}^r \cdot sk_s \bmod p)$, $i=1,2,\ldots,n$.

3). Compute the message to be sent, $M = (m_1 \oplus x_1) \| \cdots\cdots \| (m_n \oplus x_n)$, where m_i is the message which will be sent to receiver *i*.

4). Compute $y = g^x \bmod p$ and $K = h_2(y)$.

5). Compute $C = Enc_K(M)$.

6). Compute $v = h_3(M) \oplus y \bmod p$.

7). Compute $s = x/(v + sk_s) \bmod p$.

8). Compute $t = y - sk_s \cdot v \bmod p$.

9). Output ciphertext $\sigma = (C, v, s, t, \delta)$.

Unsigncrypt: When receiving ciphertext $\sigma = (C, v, s, t, \delta)$, the receiver *i* follows the steps below.

1). Compute $y = (pk_s \cdot g^v)^s \bmod p$.

2). Compute $K = h_2(y)$, $M = Dec_K(C)$.

3). Compute $v' = h_3(M) \oplus y \bmod p$ to decide whether $v' = v$ holds or not. If they are equal, the receiver *i* does the following steps; otherwise, the communication is stopped.

4). Compute $x_i = h_1(\delta^{sk_{ri}} \cdot \frac{y-t}{v} \bmod p)$.

5). Find the corresponding section of message, and decrypt the message belonging to receiver *i*, $m_i = (m_i \oplus x_i) \oplus x_i$.

5.2 Correctness

It is obvious that the above unsigncryption algorithm is valid. The unsigncryption of our scheme is corrected by the following :

For each *i* with $1 \le i \le n$, we have the $y = (pk_s \cdot g^v)^s \bmod p$ and $K = h_2(y)$, thus, $M = Dec_K(C)$, and $v' = h_3(M) \oplus y \bmod p$, if $v = v'$ then the message m is correct.

Furthermore:

$$x_i = h_1(\delta^{sk_{ri}} \cdot \frac{y-t}{v} \bmod p)$$

$$= h_1(\delta^{sk_{ri}} \cdot sk_s \bmod p)$$

$$= h_1(pk_{ri}^r \cdot sk_s \bmod p)$$

Get $m_i = (m_i \oplus x_i) \oplus x_i$.

6. Security Proofs

Now we prove that our scheme is IND-M-HSC-CCA2 secure, and EUF-M- HSC -CMA is secure under the GDH assumption and the DL assumption.

6.1 Confidentiality

The confidentiality is the necessary security requirement for a signcryption scheme. It means that no useful information about a plaintext message can be gleaned from the corresponding ciphtext.

Theorem 1. In the random oracle, if an adversary *A* has non-negligible advantage against the IND-M-HSC-CCA2 security of our scheme when running in time *t* and performing q_s signcryption queries, q_d unsigncryption queries and $q_i (i = 1,2,3)$ hash queries, then there is an algorithm *B* which solves the GDH problem with probability $\varepsilon' \ge \varepsilon \cdot \left[1 - \frac{q_s(q_s + 2q_d + 2q_3 - 1) + 2q_d}{2q}\right]$ within running time $t' \le t + (q_d + q_s)O(t_1)$ where t_1 denotes the time required for one discrete logarithm operation.

Proof. We show how to build an algorithm *B* to solve the GDH problem by running the adversary *A* as a subroutine. On inputting (g, g^a, g^b), the goal of *B* is to compute g^{ab}. After the game starts, *B* randomly selects v^*, $s^* \in Z_P^*$, setting $y = pk_r^x \bmod p$, $pk_s = (g^a \cdot g^{-v^* s^*})^{\frac{1}{s^*}} \bmod p$, $pk_r = g^b \bmod p$, and the goal is to compute :

$$y^* = (pk_s \cdot g^{v^*})^{s^* sk_r} \bmod p$$

$$= ((g^a g^{-v^* s^*})^{\frac{1}{s^*}} \cdot g^{v^*})^{s^* b} \bmod p$$

$$= (g^{\frac{a}{s^*}})^{s^* b} \bmod p = g^{ab} \bmod p.$$

B can simulate the challenger to execute each phase of the IND-M-HSC-CCA2 game for A as follows:

Phase1:

At the beginning of the game, *B* sets $params = (G_1, g, q, p, h_1, h_2, h_3)$ and generates *n* public / private key pairs $(pk_{r1}, sk_{r1}), (pk_{r2}, sk_{r2}), ..., (pk_{rn}, sk_{rn})$, $sk_{ri} \in Z_p^*$, $pk_{ri} = g^{sk_{ri}} \in Z_p^*$, ($i=1,2,\ldots\ldots,n$), which are sent to *A* ,where H_1, H_2, H_3 are random oracles controlled by B.

Let L_{H_1}, $L_{H_2}^1$, $L_{H_2}^2$, $L_{H_3}^1$, $L_{H_3}^2$ be used for storing the results of the querying h_1, h_2, h_3 ,respectively. During the simulation, B employs a DDH oracle, and the oracle inputs three groups of elements; if they are Diffie-Hellman tuples, then outputs symbols "$\top$" , otherwise outputs " $\perp$ ". Where DDH (g^a,g^b,g^c) denotes a DDH oracle.

H_1 queries: *A* inputs a public key $pk_{ri}\ (1 \le i \le n)$ to H_1, and *B* checks if there exists (x_i,n_i) in L_{H_1}. If such a tuple is found, *B* answers x_i; otherwise *B* randomly selects $\eta \in Z^*$,compute $x_i = h_1(pk_{ri} \cdot \eta \bmod p)$ and put(x_i,i) in L_{H_1}, and return x_i as the answer.

H_2 queries: For a H_2(y) query, *B* performs the following steps.

- If DDH(g^a, g^b, *y*) = "$\top$", then returns *y* as the answer of GDH problem;
- Otherwise, if exists (*y*, *K*) in $L_{H_2}^1$, returns *K*;
- *Otherwise, if exists* (φ , *K) in* $L_{H_2}^2$ *and DDH* (g^b, φ , *y)*= $\top$, *returns K;*
- Otherwise, *B* randomly selects $K \in \kappa$, puts (*y*, *K*) into $L_{H_2}^1$ and returns *K*.

H_3 queries: For a H_3 query, *B* performs the following steps.

- If DDH (g^a, g^b, *y*) = "$\top$", then returns *y* as the answer of GDH problem;
- Otherwise, if exists (v ,*y*) in $L_{H_3}^1$, returns *v*;
- Otherwise, if exists (φ ,*v*, *M*) in $L_{H_3}^2$ and DDH(g^b, φ , *y*)= $\top$, returns *v* ;
- Otherwise, *B* randomly selects $v \in Z_p^*$, puts (*v*, *y*) into $L_{H_3}^1$ and returns *v*.

Signcryption queries: For a signcryption query on plaintext $(m_1, m_2, ..., m_n) \in G_1$ chosen by the adversary *A*, *B* first randomly chooses *r*, $x \in Z_P^*$, computes $\delta = g^r \bmod p$, runs the H_1 simulation process to obtain x_i $(i = 1, 2, ..., n)$ and computes $M = (m_1 \oplus x_1 \| ..... \| m_n \oplus x_n)$. Computes $y = g^x \bmod p$ and obtains *K* from $L_{H_2}^1$ or $L_{H_2}^2$. Then computes $C = Enc_K(M)$. Checks if there exists (*v*, *y*) in $L_{H_3}^1$ or (φ ,*v*, *M*) in $L_{H_3}^2$; if tuple is not found, the game ends; otherwise, reads *v*, computes $s = x/(v + sk_s) \bmod p$, $t = y - sk_s \cdot v \bmod p$, and returns $\sigma^* = (C, v, s, t, \delta)$ to *A*.

Unsigncryption queries: For an unsigncryption query on a ciphertext (C, v, s, t, δ) and a sender's public key pk_s, both chosen by *A*, *B* does the following:

B computes $\varphi = (pk_s \cdot g^v)^s \bmod p$.

- If $\varphi = g^a$, the $\perp$ symbol is returned to *A* and the game is stopped ;
- If $L_{H_3}^1$ contains a tuple (y, v') and $M = M'$, $DDH(g^b, \varphi, y) = \top$, but $v \ne v'$, the $\perp$ symbol is returned to *A* and the game is stopped;
- Otherwise, if $L_{H_3}^2$ contains a tuple (φ', M, v') and $\varphi = \varphi'$, $M = M'$, but $v \ne v'$, the $\perp$ symbol is returned to *A* and the game is stopped;
- Otherwise, randomly chooses $r' \in Z_P^*$, puts (φ, M, v') into L_{H3}^2.
- If L_{H2}^1 contains a tuple (*y*,*K*), and $DDH(g^b, \varphi, y) = \top$, returns *K* to *A*;
- Otherwise, if L_{H2}^2 contains a tuple (φ', *K*), and, $\varphi = \varphi'$, returns *K* to *A*;
- Otherwise, randomly chooses $K \in \kappa$, puts (φ, *K*) into L_{H2}^2 and returns *K*.
- Computes $M = Dec_K(C)$, obtains x_i from L_{H1},then, gets m_i.

Challenge: *A* decides to stage 1 when stop and into the challenge. *A* chooses a target plaintext ($m_0^* = \{m_1, m_2, ..., m_n\} \in G_1$, $m_1^* = \{m_1', m_2', ..., m_n'\} \in G_1$), *B* does the following:

B randomly selects $b \in \{0,1\}$ to calculate M^*, $y = pk_r^x \bmod p$. Finally, *B* generates the ciphertext $\sigma^* \leftarrow Signcrypt(m_b^*, sk_s, pk_{r1}^*, pk_{r2}^*, ..., pk_{rn}^*)$ and sends σ^* to *A*.

Phase 2: *A* makes some new queries as in the first stage with the restriction that it can't query the unsigncryption oracle with σ^* .

Guess: *A* outputs a bit *b'* and wins if *b'*=*b*.

If *A* wins the game, then *B* can compute:

$$y = (pk_s \cdot g^v)^{s \cdot sk_r} \bmod p$$

$$= ((g^a g^{-v \cdot s})^{\frac{1}{s}} \cdot g^v)^{s \cdot b} \bmod p = g^{ab} \bmod p .$$

The GDH problem is solved, which is inconsistent with the assumptions.

In signcryption inquiry, it may cause a conflict that *B* adds (φ, M, v) to L_{H3}^2. In addition, L_{H3}^1 and L_{H3}^2 lists have at most $q_3 + q_d$ items in the first phase. *B* will add an entry to the L_{H3}^2 in every query. For the q_s signcryption query, B will fail with a

$\frac{q_s(q_s+2q_d+2q_3-1)}{2q}$ probability. For the q_d unsigncryption inquiry, *B* may reject a legitimate ciphertext, the probability of occurrence of this event is at most q_d/q.Therefore, the total probability which *B* failure is $\frac{q_s(q_s+2q_d+2q_3-1)+2q_d}{2q}$.Consequently, B solves the GDH problem with probability $\varepsilon' \geq \varepsilon \cdot \left| 1-\frac{q_s(q_s+2q_d+2q_3-1)+2q_d}{2q} \right|$.

6.2 Unforgeability

Unforgeability of M-HSC scheme is based on Discrete Logarithm (DL) Problem, and specific analysis is as follows.

Theorem 2. In the random oracle, if an forger *F* has non-negligible advantage against the EUF-M-HSC-CMA security of our scheme when running in time *t* and performing q_s signcryption queries and $q_i(i=1,2,3)$ hash queries ,then there is an algorithm *B* that solves the DL problem with probability $\varepsilon' \geq \varepsilon \cdot \frac{q_s(2q_2+2q_3+q_s-1)}{2q}$ within running time $t' \leq t + (t_f+q_s)O(t_1)$ where t_1 denotes the time required for one discrete logarithm operation.

Proof. We will show how to build an algorithm *B* to solve the DL problem by running the forger *F* as a subroutine. On inputting (g^a, y), $y \in G_1$, the goal of *B* is looking for a $(0 \leq a \leq q, g^a = y)$.

Initialization: *B* sends system parameters to *F* and generates *n* public / private key pairs (pk_s, sk_s), $(pk_{r1}, sk_{r1}), (pk_{r2}, sk_{r2}), ..., (pk_{rn}, sk_{rn})$,where $sk_s, sk_{ri} \in Z_p^*$, $pk_s = g^{sk_s}, pk_{ri} = g^{sk_{ri}} \in Z_p^*$, （ $i=1,2,\ldots\ldots,n$ ） . *B* returns $(pk_s, pk_{r1}, ..., pk_{rn}, sk_{r1}, ..., sk_{rn})$ to *F*.

Attack: *F* performs some polynomial bounded hash queries and signcryption queries. *B* can simulate the challenger to execute each phase of the EUF-M-HSC-CMA game for *F* as follows:

Let L_1, L_2, L_3 be used to store the results of the queries H_1, H_2, H_3 respectively, where h_1, h_2, h_3 are random oracles controlled by *B*.

H_1 queries: Inputs a public key $pk_{ri}(1 \leq i \leq n)$ to H_1, *B* checks if there exists (x_i,n_i) and $n_i = i$ in L_1. If such a tuple is found, *B* answers x_i; otherwise *B* randomly selects $\eta \in Z^*$, computes $x_i = h_1(pk_{ri} \cdot \eta \bmod p)$ and puts (x_i,i) into L_1 , and returns x_i as the answer.

H_2 queries: *B* checks if there exists (*y*,*K*) in L_2. If such a tuple is found, *B* answers *K*; otherwise *B* randomly selects $K \in \kappa$, puts (*y*,*K*) into L_2 and returns *K* to *F*.

H_3 queries: *B* checks if there exists (*M*,*y*,*v*) in L_3. If such a tuple is found, *B* answers *v*; otherwise *B* computes $z \equiv y \bmod p$, submits (*M*,*z*) to H_3 oracle, and then puts(*M*,*z*,*v*) into L_3 and returns *v* to *F*.

Signcryption queries: *F* produces messages $(m_1, m_2, ..., m_n) \in G_1$, *B* first randomly chooses $r \in Z_p^*$, computes $\delta = g^r \bmod p$, runs the H_1 simulation process to obtain x_i $(i=1,2,....., n)$ and computes $M = (m_1 \oplus x_1 \| ..... \| m_n \oplus x_n)$. *M* is submitted to the signcryption oracle for obtaining (v, s, t). *B* computes $z = (pk_s g^v)^s \bmod p$, $C = Enc_K(M)$, puts (*z*,*K*) into L_2 and puts(*M*,*z*,*v*) into L_3, and returns $\sigma = (C, v, s, t, \delta)$ to *F*.

Forge: *F* produces a ciphertext σ^* and gives an arbitrary sender's public key pk_u .The σ^* is a valid ciphertext if the result of $Unsigncrypt(\sigma^*, pk_u, sk_{ri})(1 \leq i \leq n)$ is not "$\perp$". In the meanwhile, *F* can't do $Signcrypt(m^*, sk_u, pk_{r1}, pk_{r2}, ..., pk_{rn})$.

Analysis:

The case which σ^* is a valid ciphertext and indicates that *B* knows $g^a = g^{(sk_s+v)\cdot s} = (pk_s \cdot g^v)^s = y$, in other words, $a = (sk_s + v) \cdot s$, which is inconsistent with the assumptions.

In the game, the only thing that might fail is querying the values of H_2 and H_3 in signcryption queries. Because *F* does a maximum of q_2 H_2-queries and q_3 H_3-queries, possible number of different *y* is stored at most is $q_2 + q_3$.In the *i* signcryption query, *y* inconsistent probability is at most $\frac{q_2+q_3+(i-1)}{q}$. *F* runs q_s-times signcryption queries as far as possible, so the probability of *F* success is $\varepsilon' \geq \varepsilon \cdot \frac{q_s(2q_2+2q_3+q_s-1)}{2q}$.

6.3 Efficiency Analysis

When the sender sends *n* messages to *n* receivers, the length of the ciphertext in our scheme is $|nm| + 4|G_1|$. The length of the ciphertext is $n(|m| + (n+2)|G_1|)$ of Ref.[4], which is larger than the length of the proposed scheme in this paper. In Ref.[16], the signcryption process requires three multiplication operations and its length of ciphertext is $(|nm| + 2|G_1| + n|G_2|)$. Therefore, it is longer than the one of this paper and does not facilitate transmission. In conclusion, compared with the existing schemes, the ciphertext of the proposed scheme is shorter. In our scheme, signcryption operation requires 0 pairing operation, *n* multiplications and (*n*+2) hash

operations, but unsigncryption operation requires 0 pairing operation, *2* multiplications and 3 hash operations for a single receiver. Comparing with previous schemes, the efficiency of this scheme is better.

Table 1 compares M-HSC with schemes of Ref.[4], Ref.[15] and Ref.[16] in computational costs and communication overheads, where $|G_1|$ indicates the length of the element in the G_1, $|G_2|$ indicates the length of the element in the G_2, $|m|$ indicates the length of the plaintext message *m*.

Table 1: Efficiency comparison between M-HSC and other schemes

Scheme	Signcryption (*n* receivers, *n* messages)			Unsigncryption (single receiver)			Ciphertext size
	Pair	Mul	Hash	Pair	Mul	Hash	
Ref.[4]	0	$n(n+2)$	$n(n+2)$	$2n$	n	$3n$	$n(\|m\|+(n+2)\|G_1\|)$
Ref.[15]	0	n	$n(n+2)$	0	n	$3n$	$n(\|m\|+3\|G_1\|)$
Ref.[16]	n	3	$3n+1$	1	3	3	$(\|nm\|+2\|G_1\|+n\|G_2\|)$
M-HSC	0	n	$n+2$	0	2	3	$\|nm\|+4\|G_1\|$

7. The Application of M-HSC in CATV Networks

With the wide use of the CATV, the security issues in the network become increasingly prominent. The business and consumers are very concerned about the topic how to establish a safe, convenient environment of CATV network and provide adequate protection to the user. We present a new broadcast service protocol using M-HSC scheme, which not only can effectively broadcast information, but also can prevent the possibility of fraud and destructive behavior. The protocol consists of three phases： system initialization, broadcast service and service certification.

System initialization. The on-line or off-line KGC for CATV networks generates system parameters $params=(G_1, g, q, p, h_1, h_2, h_3)$, and operators' public/private key pair (pk_s, sk_s) and users' public/private key pairs $(pk_{r1}, sk_{r1}), (pk_{r2}, sk_{r2}), ..., (pk_{rn}, sk_{rn})$ as described in the Section 5.

Broadcast Service. Each operator can simultaneously provide a number of different services for different users. Before broadcasting messages, the operator knows the users' public key, and the user has paid related fees. The procedure of broadcasting services is depicted in Fig.1.

Step1: The operators *A* determines the set of users $\{R_1, R_2, ..., R_l\}$ and the set of services $\{m_1, m_2, ..., m_l\}, l \le n$, where *n* is the total number of users.

Step 2: *A* generates ciphertext σ as described in Section 5.

Step3: *A* sends σ to $\{R_1, R_2, ..., R_l\}$ via a secure channel.

Service Certification. The user can authenticate the received broadcast messages by employing our scheme. The user can verify whether the received message is correct and intact. Fig.2 shows how a legitimate user obtains services provided by the operator.

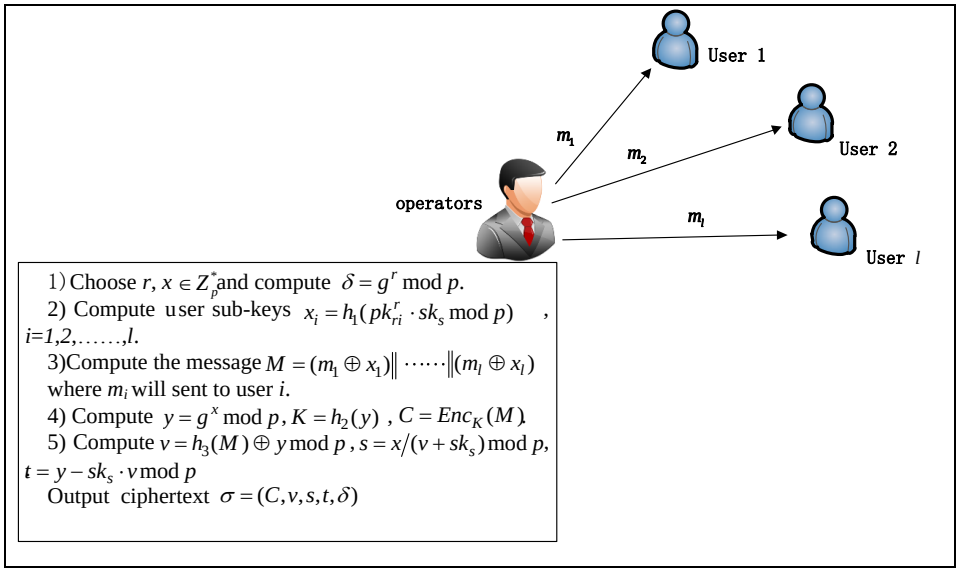

Figure 1: Broadcast services of operators

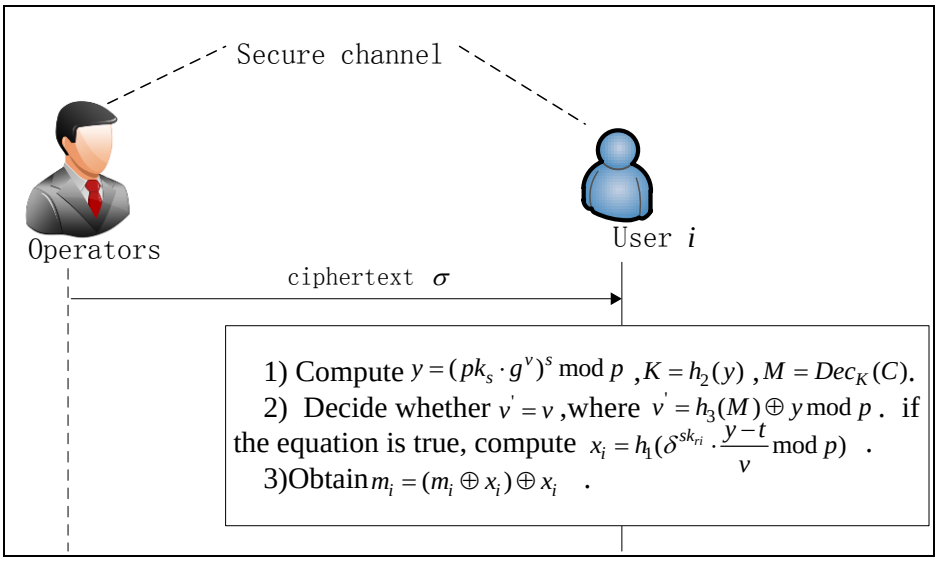

Figure 2: Obtain service of legitimate user

8. Conclusions

In this paper, based on the discrete logarithm and GDH problem, we present a multi-message and multi-receiver hybrid signcryption scheme. Under the random oracle model, the formal demonstration shows that the proposed scheme can meet the indistinguishability of multi-message and multi-receiver hybrid signcryption, chosen ciphertext attack (IND-M-HSC-CCA2) and existentially unforgeable against chosen message attack (EUF-M-HSC-CMA). The analysis shows that our scheme not only is secure, reliable and verifiable, but also meets the fairness of decryption to prevent possible cheating behavior of the sender effectively. At the same time, the scheme can meet the requirement of businessmen where one signcryption operation will broadcast a number of different services to multiple receivers in the CATV networks environment.

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